

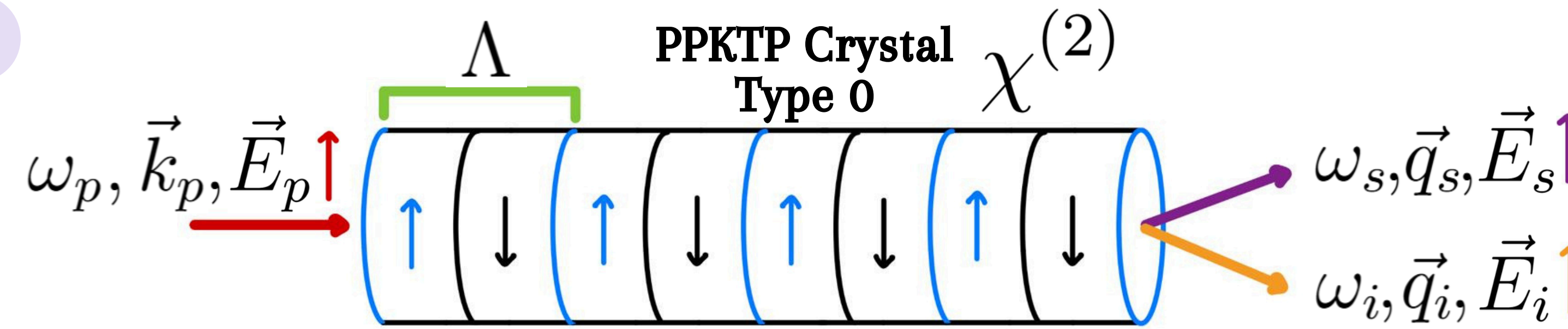
# Exploring Entanglement in Photon Pairs Generated by PPKTP Nonlinear Crystals

## Abstract

Spontaneous Parametric Down-Conversion (SPDC) in periodically poled Potassium Titanyl Phosphate (PPKTP) nonlinear crystals is a prominent method for generating entangled photon pairs for quantum information technologies. We quantify entanglement and optimize temperature tuning for collinear emission and degenerate spectra. We analyzed Joint Spectrum Intensity (JSI) at different temperatures. Successfully extracted the Schmidt number ( $K$ ) by applying a Gaussian fit and Singular Value Decomposition (SVD).

### Spontaneous Parametric Down-Conversion

A monochromatic pump photon converts into a correlated signal-idler pair, generating an entangled two-photon state.



Quasi-Phase-Matching (QPM) conditions are obtained.

$$\Delta k_{\text{QPM}} = k_p - k_s - k_i - \frac{2\pi}{\Lambda} \approx 0 \quad \text{Momentum}$$

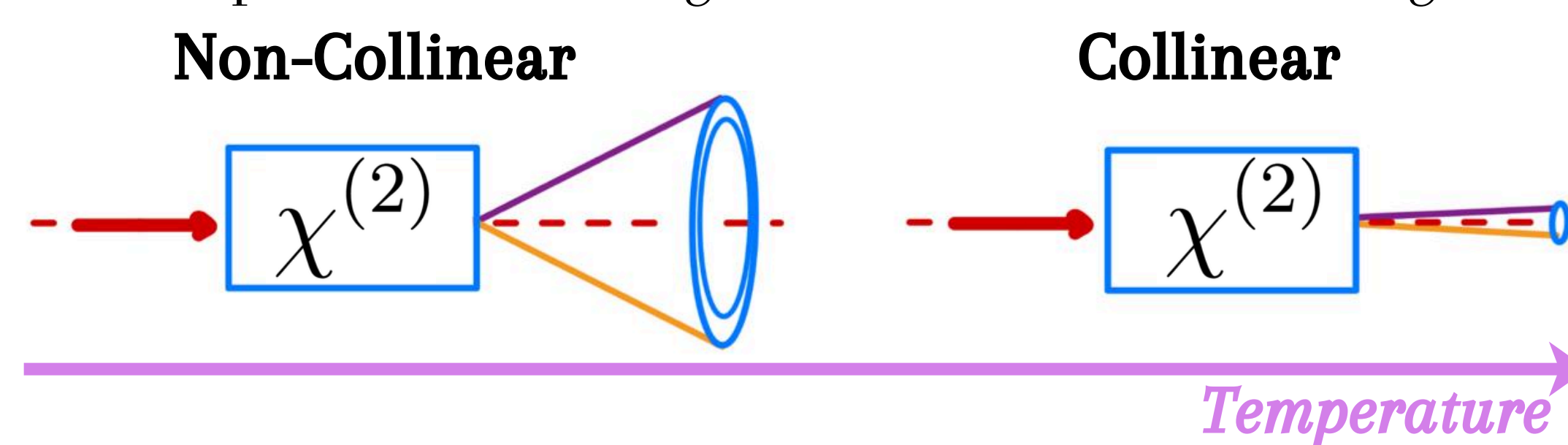
$$\omega_p = \omega_s + \omega_i \quad \text{Energy}$$

$$\text{Biphoton state} \rightarrow |\Psi\rangle = |0\rangle + \int d^2\vec{q}_s \int d^2\vec{q}_i \int d\omega_s \int d\omega_i \Psi(\omega_s, \vec{q}_s, \omega_i, \vec{q}_i) \hat{a}_s^\dagger(\omega_s, \vec{q}_s) \hat{a}_i^\dagger(\omega_i, \vec{q}_i) |0\rangle$$

Correlations in continuous variables.

### Temperature Tuning

The crystal's poling period,  $\Lambda(T)$ , is highly dependent on temperature, leading to different emission regimes.



### Entanglement Quantification

SVD is performed on the target state to obtain the Schmidt decomposition

$$\Psi(\omega_s, \vec{q}_s, \omega_i, \vec{q}_i) = \sum_{k=0}^{\infty} \sqrt{\lambda_k} u_k(\omega_s, \vec{q}_s) v_k(\omega_i, \vec{q}_i)$$

We are focus on time-frequency correlations.

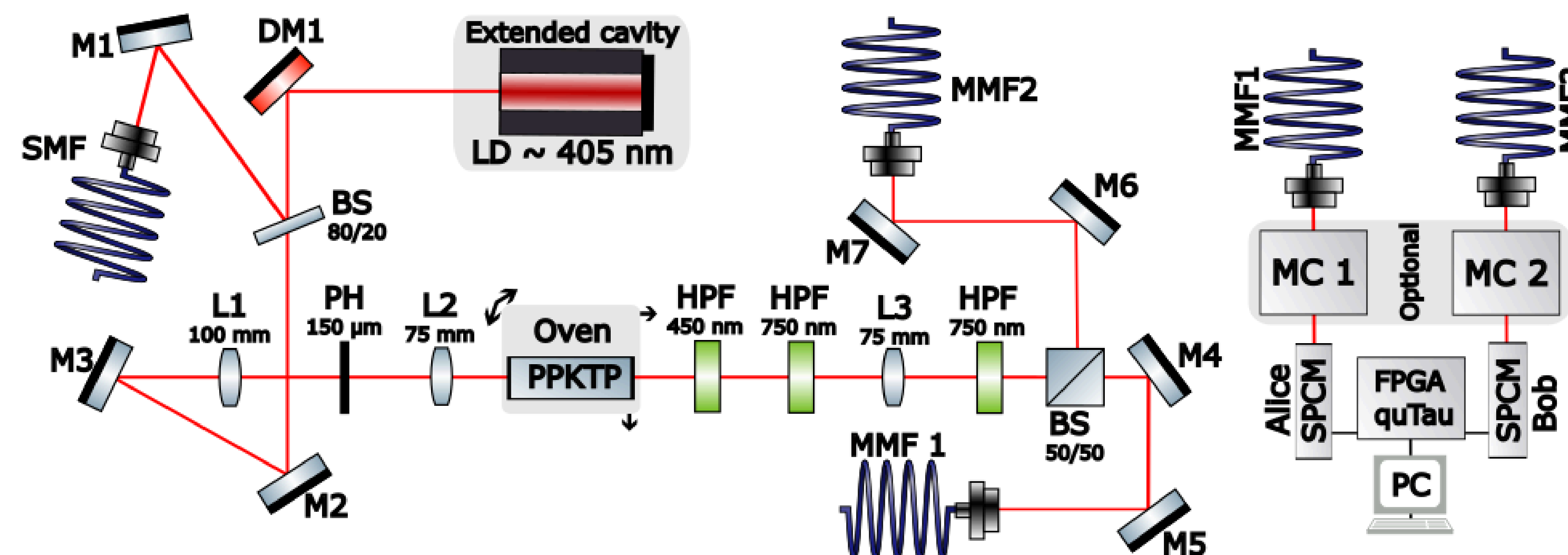
$$\psi(\omega_s, \omega_i) \rightarrow K_\omega \quad \psi(\vec{q}_s, \vec{q}_i) \rightarrow K_{\vec{q}} \quad K_{\text{full}} \neq K_\omega \cdot K_{\vec{q}}$$

Schmidt Number quantify quantum correlations.

$$K = \frac{1}{\sum_k \lambda_k^2}$$

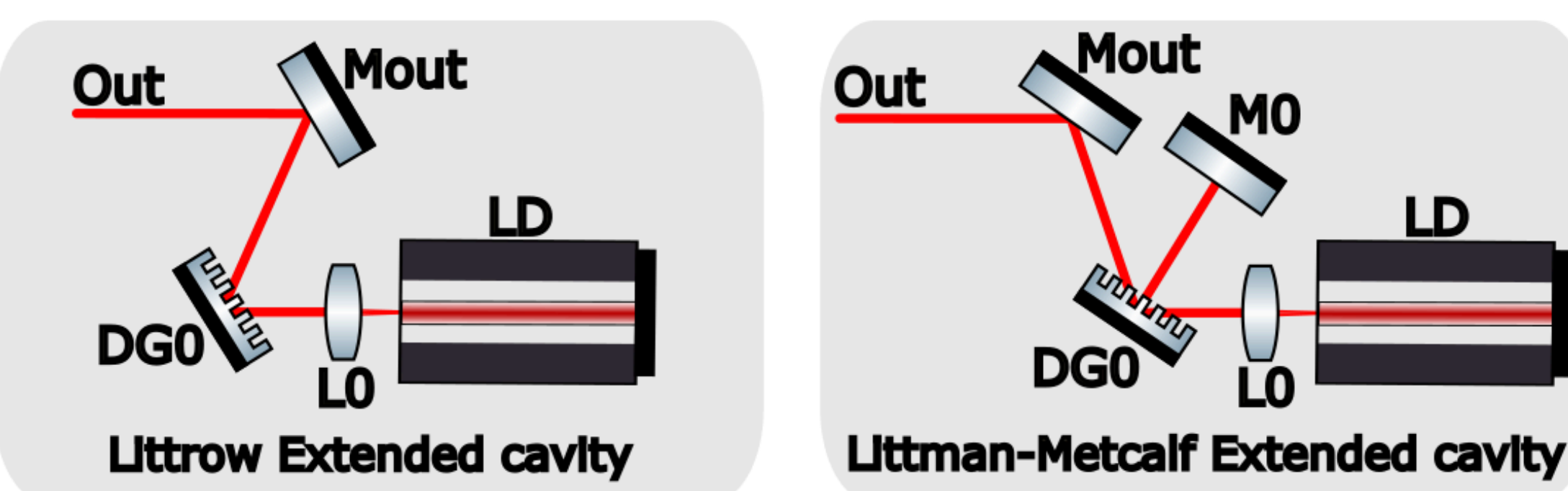
$K = 1 \rightarrow$  Product State  
 $K > 1 \rightarrow$  Entangled State

## Experimental Setup



Our PPKTP Crystal is extremely sensible to wavelength variations.

We build an extended cavity that allows a single-mode behavior on our pump source.

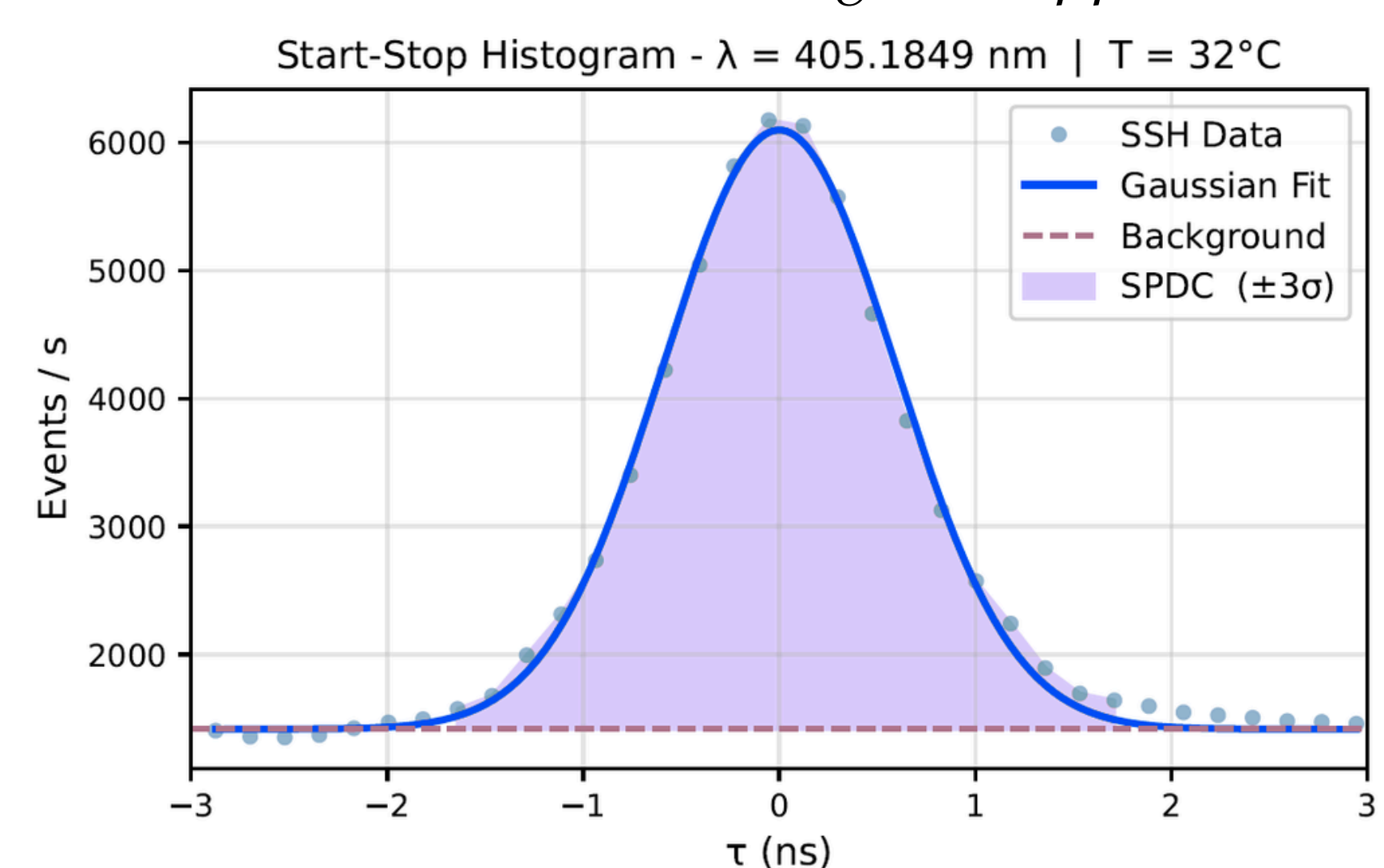
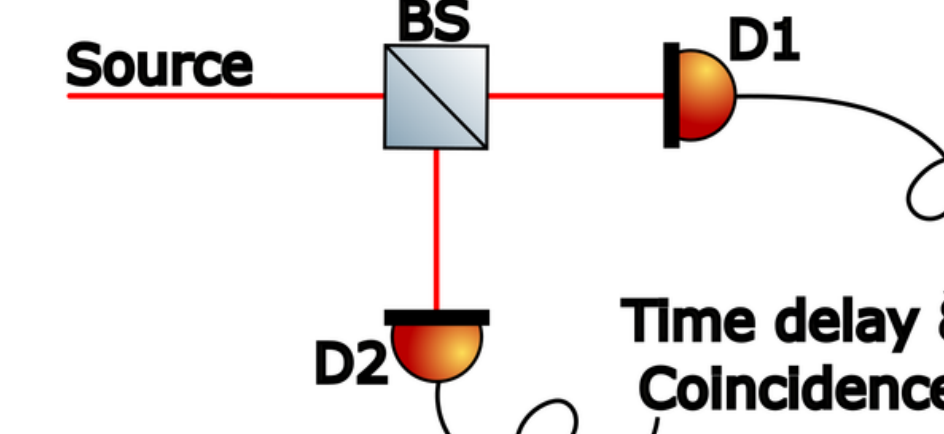


Detection Signal-idler photon correlations are evaluated using two approaches

### Temporal

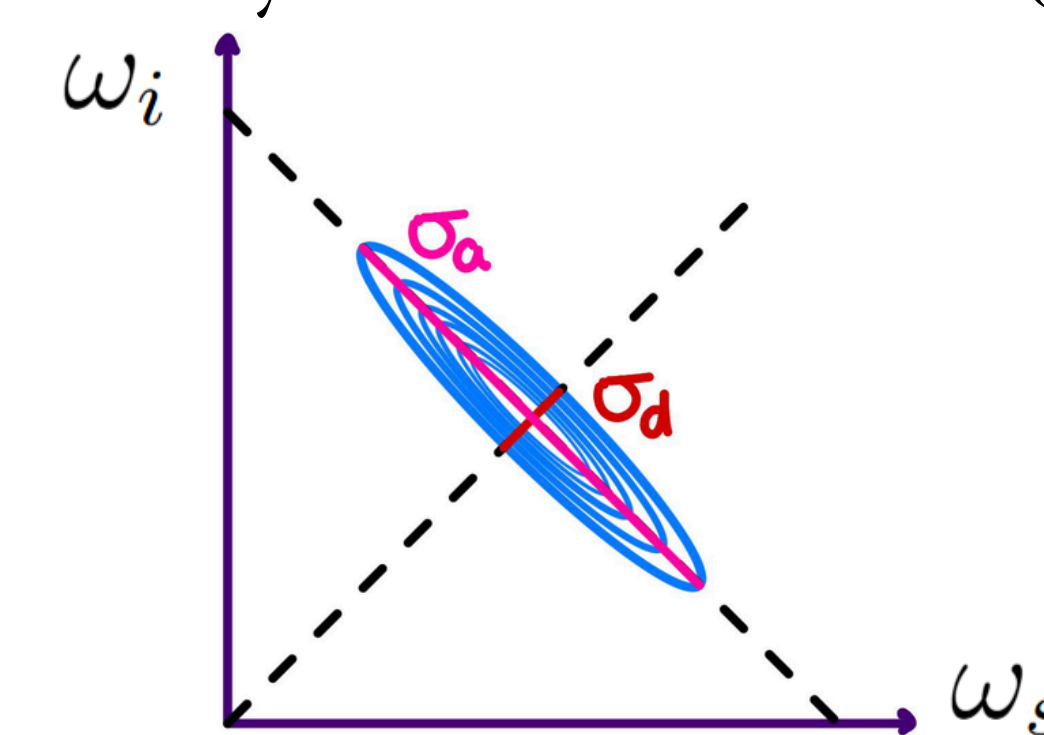
A HBT interferometer measures the second order correlation function.

$$g^{(2)}(\tau) = \frac{\langle \hat{E}_s^\dagger(t+\tau) \hat{E}_i^\dagger(t) \hat{E}_i(t) \hat{E}_s(t+\tau) \rangle}{\langle \hat{E}_s^\dagger(t+\tau) \hat{E}_s(t+\tau) \rangle \langle \hat{E}_i^\dagger(t) \hat{E}_i(t) \rangle}$$



### Spectral

Two monochromators measure the JSI. Maps photon coincidences as a 2D probability distribution over  $(\lambda_s, \lambda_i)$ .



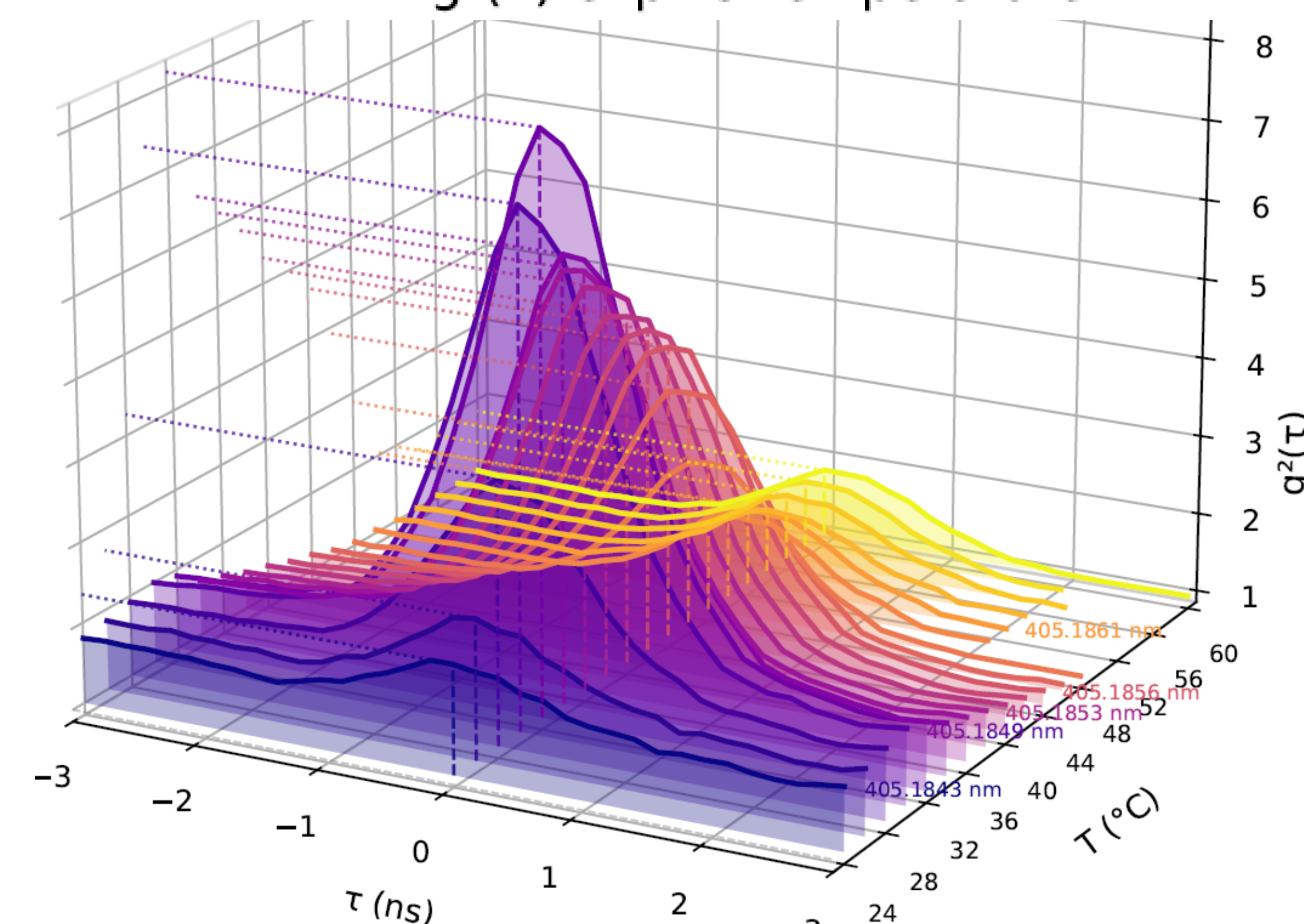
For a non-collinear emission, and supposing a gaussian spectral amplitude in the pump:

$$f(\nu_s, \nu_i) = A \exp \left\{ -(\nu_s^2 + \nu_i^2) \left( \frac{1}{4\sigma_d^2} + \frac{1}{4\sigma_a^2} \right) - 2\nu_s \nu_i \left( \frac{1}{4\sigma_d^2} - \frac{1}{4\sigma_a^2} \right) \right\}$$

$$\rightarrow K_\omega \approx \frac{\sigma_d^2 + \sigma_a^2}{2\sigma_d \sigma_a} \quad \text{Spectral Schmidt Number}$$

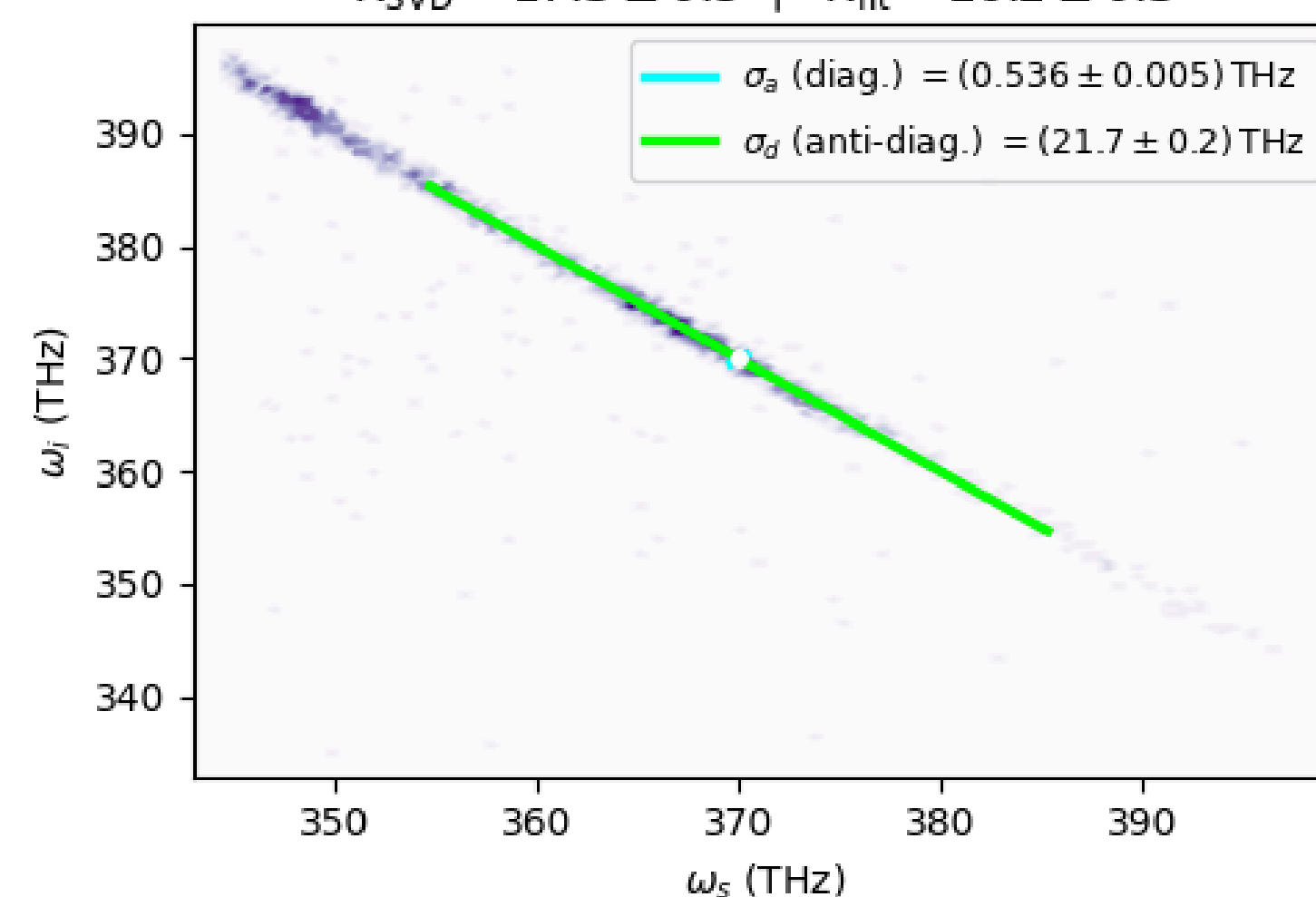
## Results and Analysis

### HBT — $g^{(2)}(\tau)$ exp vs Temperature

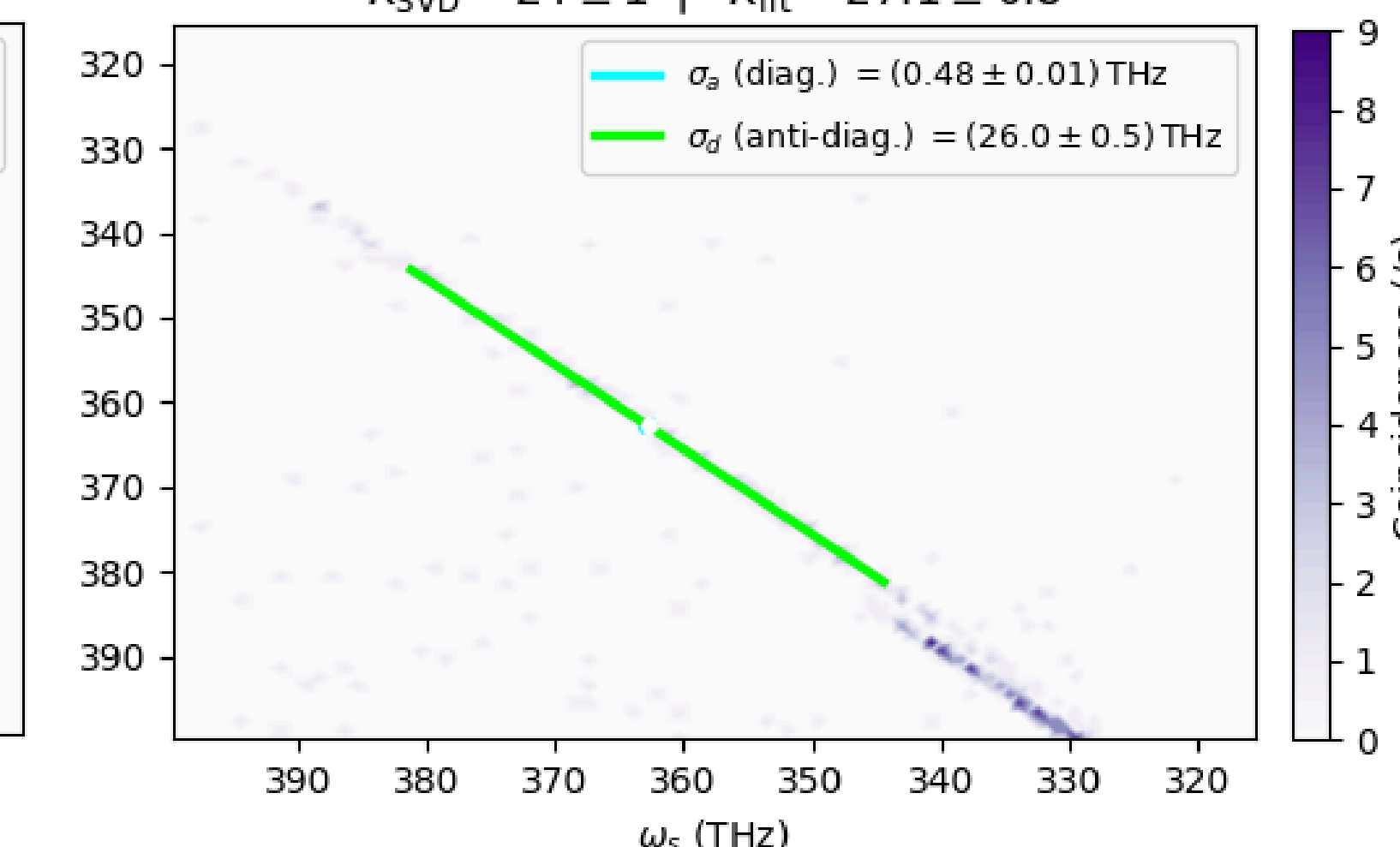


Experimental  $g^{(2)}(\tau)$  for different temperatures.  $\lambda$  changes due to laser instability.

JSI (Ehimar Vargas) PPKTP  $T = 30^\circ\text{C}$ ,  $\lambda_p = 405.1698 \text{ nm}$   
 $K_{\text{SVD}} = 17.3 \pm 0.5 \quad K_{\text{fit}} = 20.2 \pm 0.3$

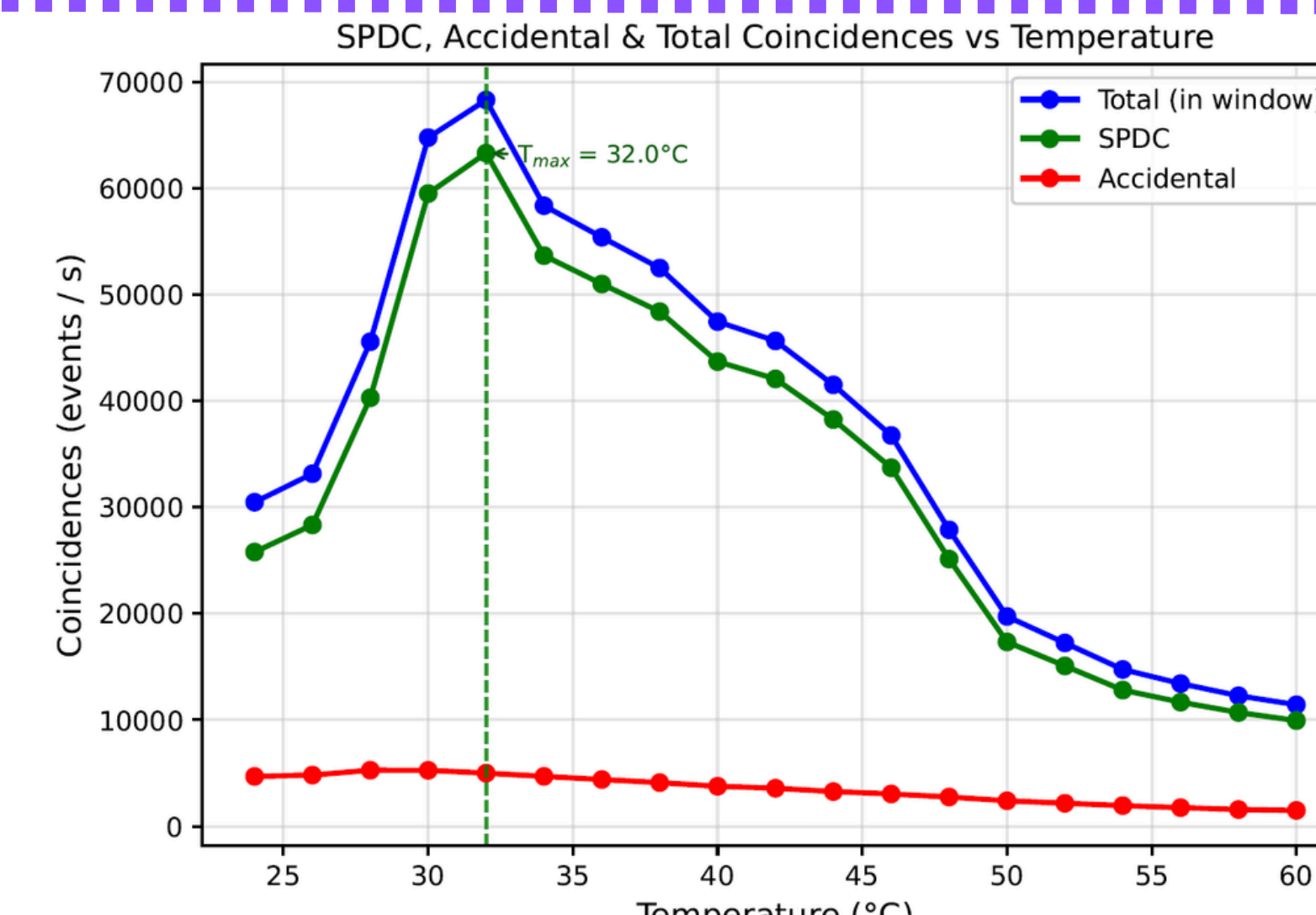


JSI (Camilo Pinilla) BBO Collinear  $\lambda_p = 411.3113 \text{ nm}$   
 $K_{\text{SVD}} = 24 \pm 1 \quad K_{\text{fit}} = 27.1 \pm 0.8$



JSI for PPKTP and BBO non-linear crystals measured by Ehimar Vargas (Uniandes) and Camilo Pinilla (Uniandes) respectively

Coincidences for different temperatures. Maximum SPDC events/s at  $T_c$ . Data collected from HBT Start-Stop Histogram



## Conclusions

- Experimentally validated signal-idler temporal correlations through  $g^{(2)}(\tau)$  measurements.
- Characterized the dependence of coincidences on crystal temperature.
- Successfully extracted the Schmidt number to quantify frequency correlations from SVD and fit approximation.
- Future Work:** Investigate entanglement in additional degrees of freedom and explore temperature sweep ranges to further map the emission regimes.

## References

- [1] Kevin Zielnicki et al. «Joint spectral characterization of photon-pair sources». Journal of Modern Optics 65.10 (2018), págs. 1141-1160. <https://doi.org/10.1080/09500340.2018.1437228>.
- [2] H. Di Lorenzo Pires, C. H. Monken y M. P. van Exter. «Direct measurement of transverse-mode entanglement in two-photon states». Physical Review A 80 (2009), 022307.
- [3] C. Couteau. «Spontaneous parametric down-conversion». Contemporary Physics 59, 291 (2018), <https://doi.org/10.1080/00107514.2018.1488463>.
- [4] J. F. Suárez Pérez, Control experimental de las correlaciones en frecuencia de pares de fotones para una fuente de fotones individuales anunciados, Master's thesis, Universidad de los Andes, 2018, <https://hdl.handle.net/1992/34528>.